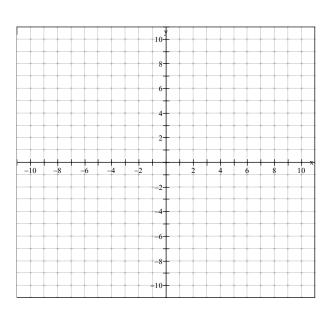
Algorithm for Maximum or Minimum (Extreme Values)

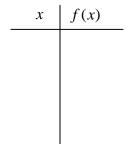
If a function f(x) has a derivative at every point in the interval $a \le x \le b$, calculate f(x) at

- all points in the interval $a \le x \le b$ where f'(x) = 0;
- the end points x = a and x = b.

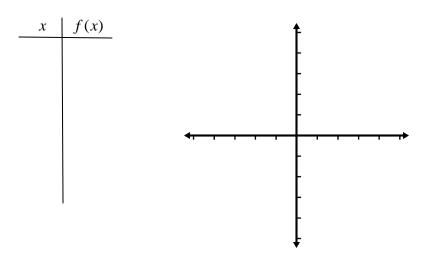
The *maximum value* of f(x) on the interval $a \le x \le b$ is the *largest* of these values, and the *minimum value* of f(x) on the interval is the *smallest* of these values.

Ex. 1. Find the *maximum* and *minimum* values(s) of f(x) for $f(x) = -2x^2 - 12x - 10$ on the interval $-4 \le x \le 0$. Illustrate graphically.





Ex. 2. Find the maximum and minimum values of the function $f(x) = x^3 - 6x^2 - 4$ for $-1 \le x \le 7$. Illustrate your results graphically.

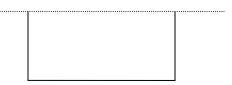


Ex. 3. A flu epidemic breaks out in Waterloo. The fraction of the population that is infected at time, t, in weeks, is given by the function $f(t) = \frac{64t}{(8+t)^3}$.

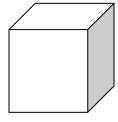
What is the largest fraction of the population that is infected during the first 10 weeks? Assume that t = 0 is when the epidemic starts.

t	f(t)

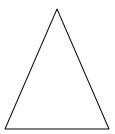
Ex. 1. A man wishes to enclose a rectangular area against the wall of a chicken house to form a chicken run. The wall is 50 m long. He has 60 m of fencing. What is the largest area he can enclose and what are its dimensions?



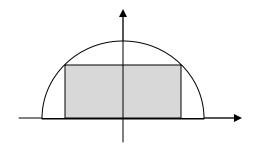
Ex. 2. An open-topped storage box is to have a square base and vertical sides. If 108 m² of sheet metal is available for its construction, find the dimensions for maximum volume.



Ex. 3. What is the maximum possible area of an isosceles triangle if the two equal sides are each 15 cm long?



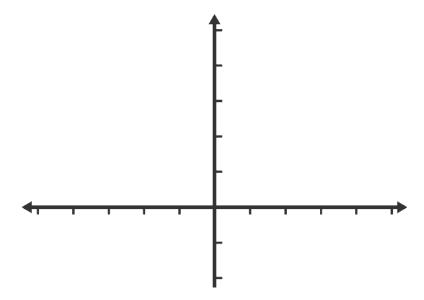
Ex. 4. Find the largest area of a rectangle inscribed in a semicircle of radius 2 cm.



Date:_____

Section 5.5 – Optimization Problems continued

Ex. 1. Find the point on the parabola $2y = x^2$ that is closest to the point (-4, 1).



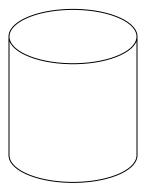
Ex. 2.	to the width of the r	is in the form of a rectangle surmounted by a semi-circle with a diameter equal rectangle. If the perimeter of the window is 14 m , what is the maximum area ne nearest tenth of a m^2 .
_		

Ex. 3. At 1:00 p.m., ship A was 80 km south of ship B. Ship A is sailing north at 30 km/h and ship B is sailing east at 40 km/h. Find when the distance between the ships is at a minimum.



Ex. 4. A manufacturer wishes to produce cylindrical fruit juice cans with a capacity of 250 ml.

- a) What dimensions will minimize the amount of material required for a can? ($1 \text{ ml} = 1 \text{ cm}^3$) Answer to the nearest tenth of a cm.
- **b**) What exact ratio of height to diameter will minimize the amount of material required.



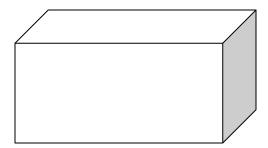
MCV 4UI - Unit 3B: Day 4

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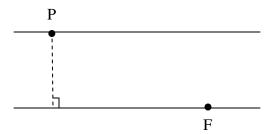
Section 5.6 – Optimizing in Economics and Science

Ex. 1. A commuter train carries 2000 passengers daily from a suburb into a large city. The cost to ride the train is \$7.00 per person. Market research shows that 40 fewer people would ride the train for each \$0.10 increase in the fare. If the capacity of the train is 2600 passengers, and contracts with the rail employees require that at least 1600 passengers be carried, what fare should the railway charge to get the largest possible revenue?

Ex. 2.	The base of a chest is a rectangle which is twice as long as it is wide. The top, front, and sides are
	made of oak, and the back and base are made of pine. The chest has a volume of 12.25 m ³ and
	oak costs three times as much as pine. Find the dimensions of the box for which the lumber has
	the lowest cost. (Neglect any effects due to the thickness of the sides, top, or base.)



Ex. 3. A powerhouse, P, is on one bank of a straight river 200 m wide, and a factory, F, is on the opposite bank, 400 m downstream from P. The cable must be run from the powerhouse to the factory at a cost of \$6/m under water and \$4/m on land. What path should be chosen so that the cost is minimized?



Ex. 4. A man lives on an island 1 km from the mainland. His favourite pub is 3 km along the shore from the point on the shore closest to the island. The man can paddle his canoe at 3 km/h and can jog at 5 km/h. Determine where he should land so as to reach the pub in the shortest possible time.

